



## ISTAGE 3 TEACHING UNIT „UNDER PRESSURE“

ACTIVITIES AND EXPERIMENTS WITH THE AIR PRESSURE INSIDE THE BALL

Corina TOMA

Philippe JEANJACQUOT

## PARTS OF THIS TEACHING UNIT



★ **PRESSURE**

★ **BOUNCE**



## PARTS OF THIS TEACHING UNIT



# ★ PRESSURE

An inventive way to study the properties of the air across the football



# PRESSURE: WHAT WE ARE GOING TO DO



## WE ARE GOING TO MEASURE:

-  The pressure inside the ball
-  The mass of the ball
-  The volume of the ball

## WE ARE GOING TO FIGURE OUT:

-  That air has a mass.
-  The link between the pressure and the mass of the air.
-  The density of the air.
-  The ideal gas law and the mass of one mole of air.

# PRESSURE: FIT TO EVERY LEVEL



## PRIMARY SCHOOL:

-  The air has a mass.

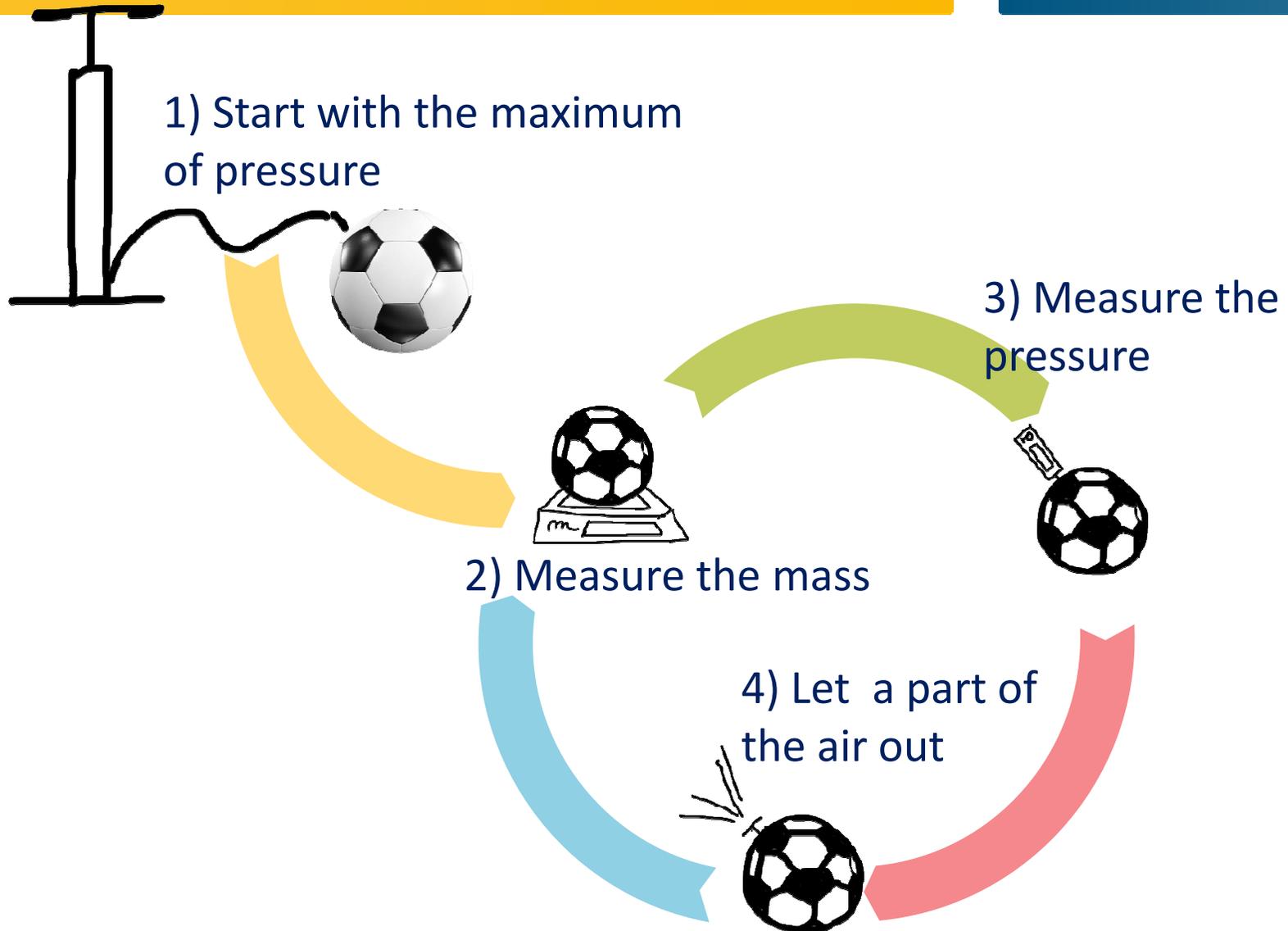
## MIDDLE SCHOOL:

-  The link between the pressure and the mass of the air.
-  Density of the air.

## HIGH SCHOOL:

-  The ideal gas law and the mass of one mole of air.
-  Show the effect of the buoyancy of the air.

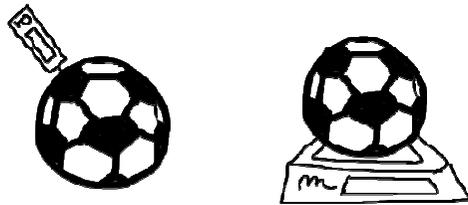
# PRESSURE: PROCEDURE



# PRESSURE: MEASURES

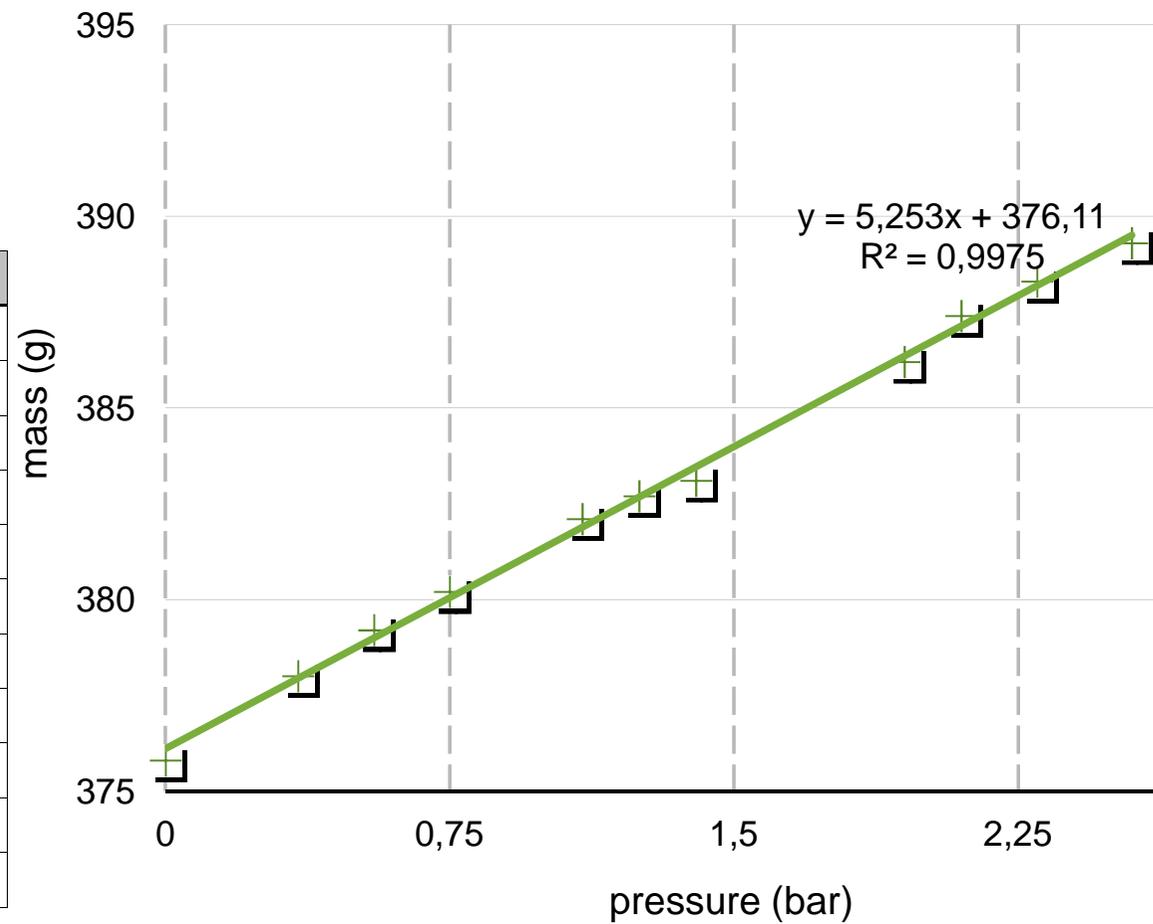


+ mass vs pressure      — BEST FIT



MASS vs. PRESSURE

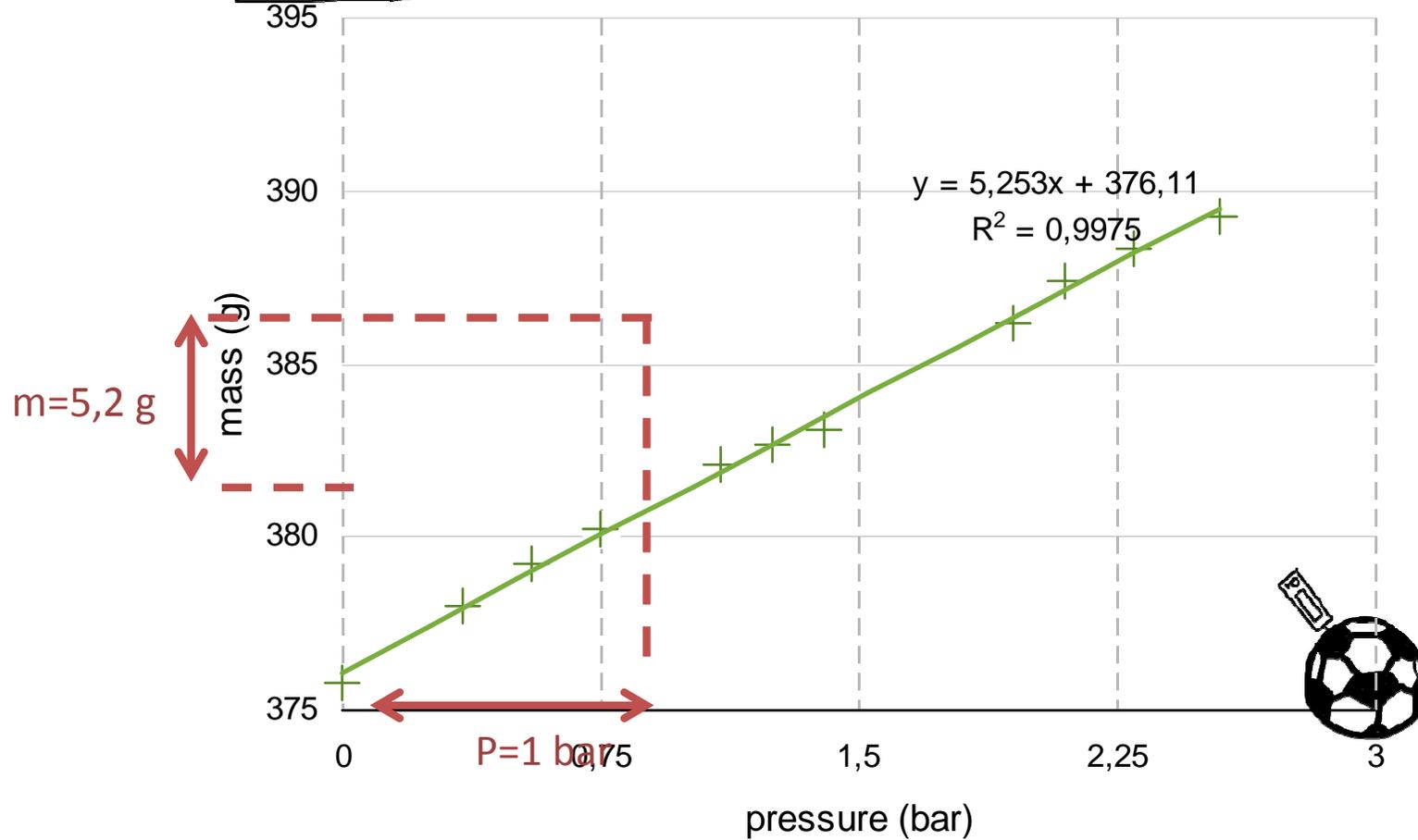
PRESSURE (bar)	MASS (g)
2.55	389.3
2.3	388.3
2.1	387.4
1.95	386.2
1.40	384.1
1.25	382.7
1.10	382.1
0.75	380.2
0.55	379.2
0.35	378
0	375.8



# PRESSURE: MASS OF AIR



+ mass vs pressure — BEST FIL



# MASS OF AIR INSIDE THE BALL

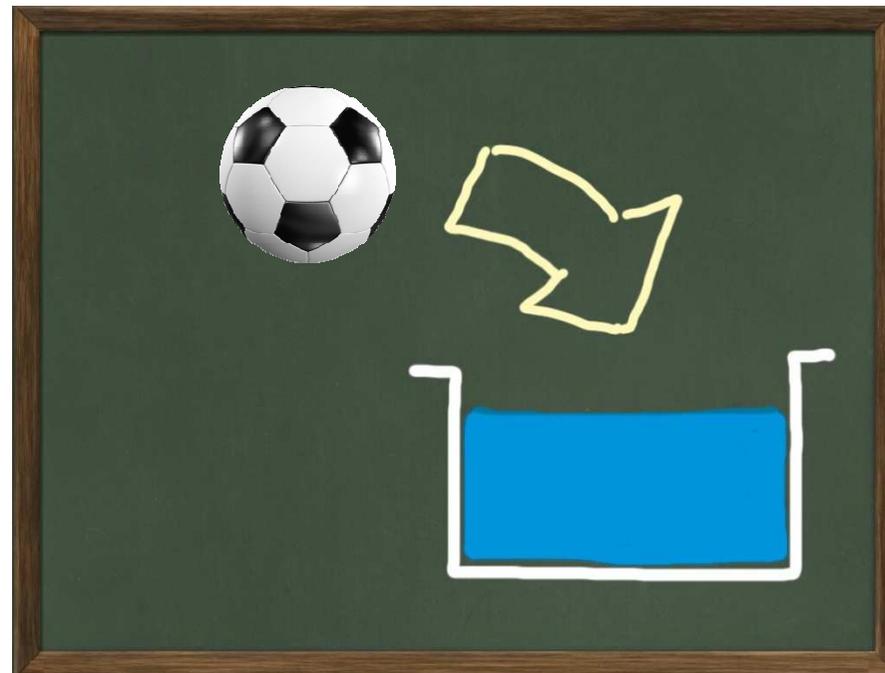


Mass of air inside the ball  
 $m = 5.2 \text{ g}$  for  $p = 1 \text{ bar}$

# VOLUME OF THE BALL



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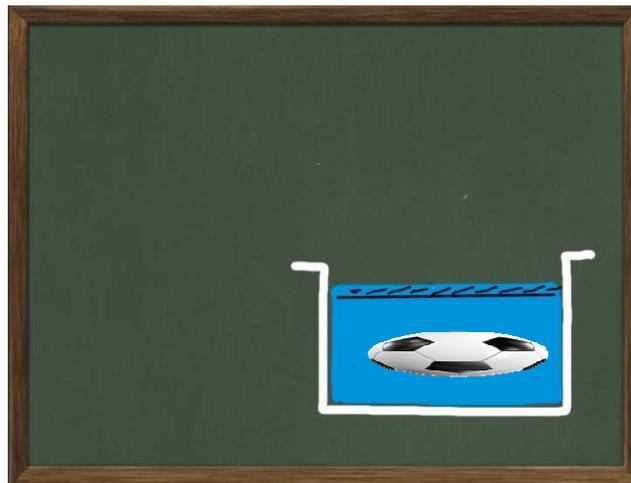
$h(\text{full}) = 5.6 \text{ cm}$



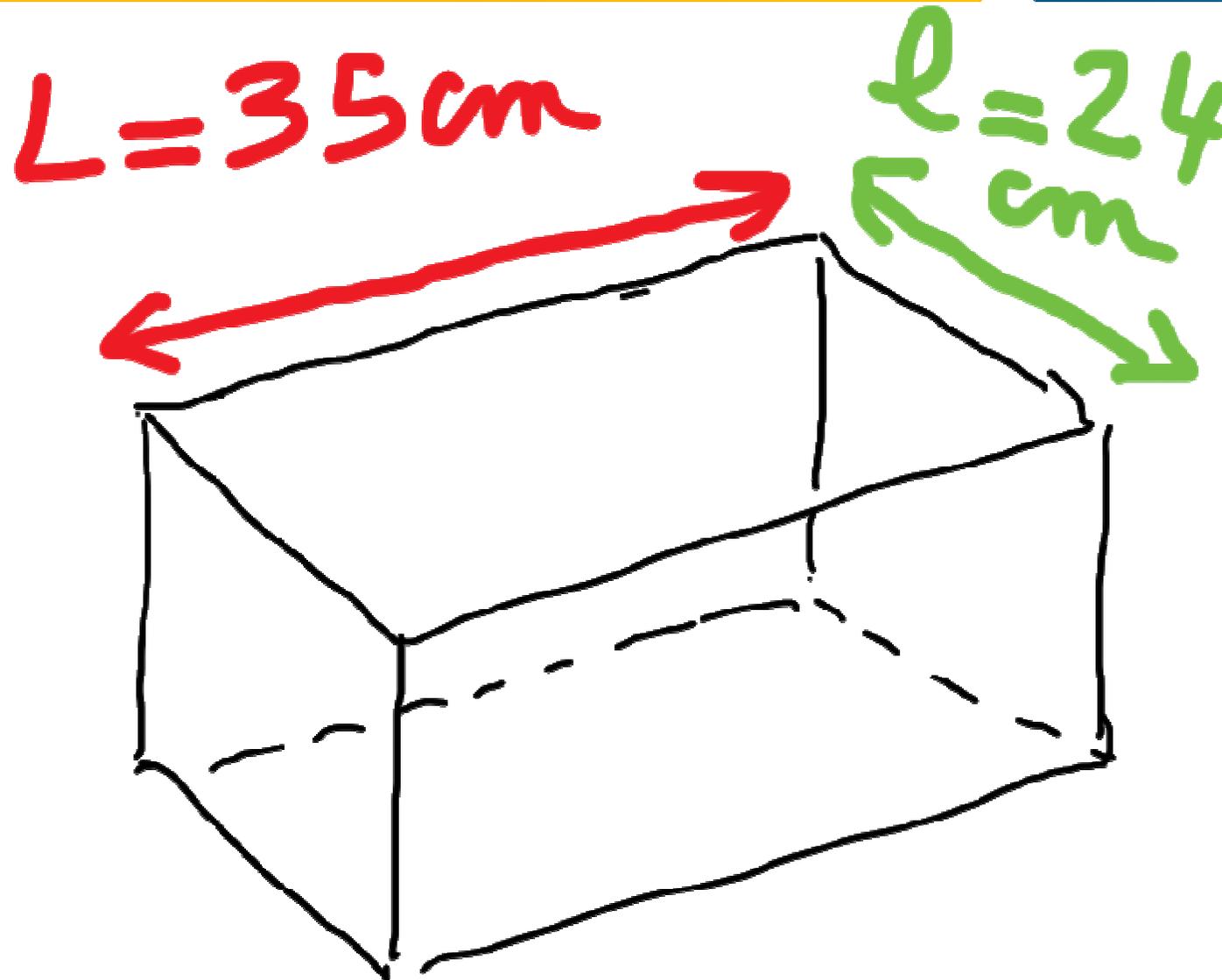
# VOLUME OF THE BALL



$h(\text{empty}) = 0.9 \text{ cm}$



# VOLUME OF THE BALL



# VOLUME OF THE BALL



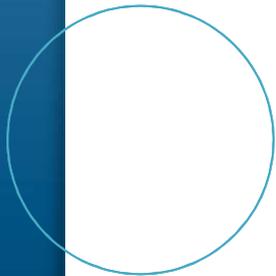
$$V(\text{full}) = 35 \times 24 \times 5.6 = 4704 \text{ cm}^3$$

$$V(\text{full}) = 4.70 \text{ L}$$



$$V(\text{empty}) = 35 \times 24 \times 0.9 = 756 \text{ cm}^3$$

$$V(\text{empty}) = 0.76 \text{ L}$$



$$V(\text{air}) = 4.70 - 0.76 = 3.94 \text{ L}$$

$$V(\text{air}) = 3.94 \text{ L}$$

# DENSITY OF THE AIR



$$d = m/v(\text{air})$$

$$d = 5.2/3.94$$

$$d = 1.32 \text{ g/L}$$

The real value is 1.2 g/L at the temperature of the measure (25°C)

The errors can occur principally from the measure of the volume (to get a good empty ball) and also from the measure of the pressure

## PARTS OF THIS TEACHING UNITS



# ★ BOUNCE



# Dependence of the bouncing height with the pressure



For an elastic collision with the ground the coefficient of restitution is:

$$e = \frac{v_{\text{separation}}}{v_{\text{approach}}}$$

$$mgh_1 = \frac{mv_{\text{approach}}^2}{2}$$

the ball is falling down from the height  $h_1$

$$mgh_2 = \frac{mv_{\text{separation}}^2}{2}$$

after the collision the ball can reach the height  $h_2$

$$e = \sqrt{\frac{h_2}{h_1}}$$

## What you need?



- ★ Football
- ★ Pump with manometer
- ★ Measuring tape or a marked paper tape that can be stuck on the wall
- ★ Smartphone
- ★ VidAnalysis application

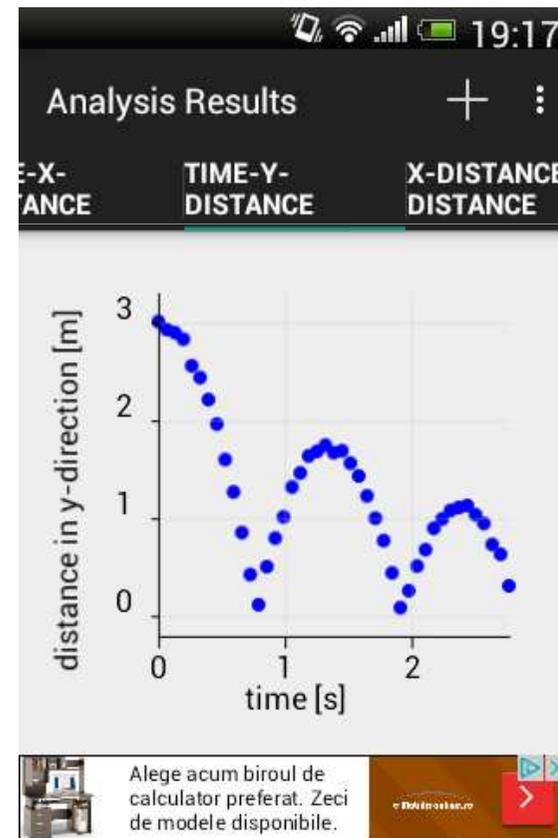
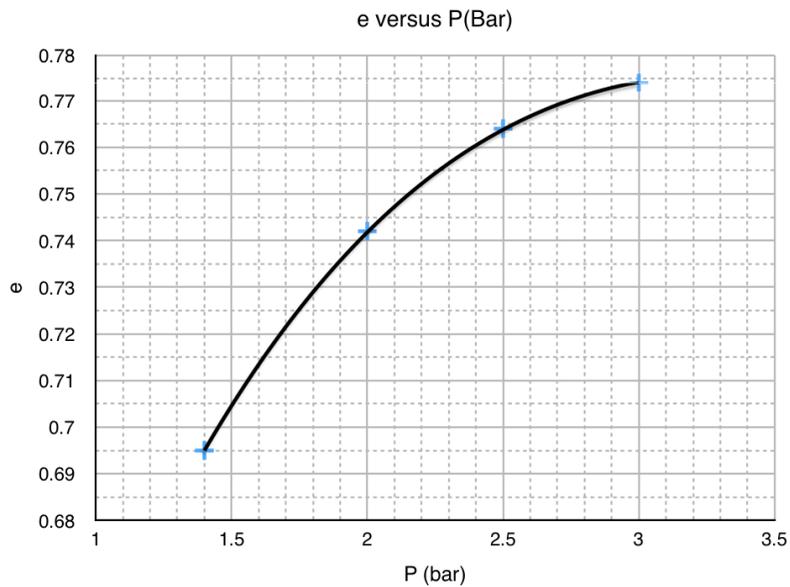
# What to do?



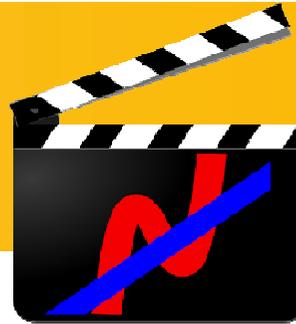
# Results



## Reading the heights from the video using VidAnalysis



# VidAnalysis



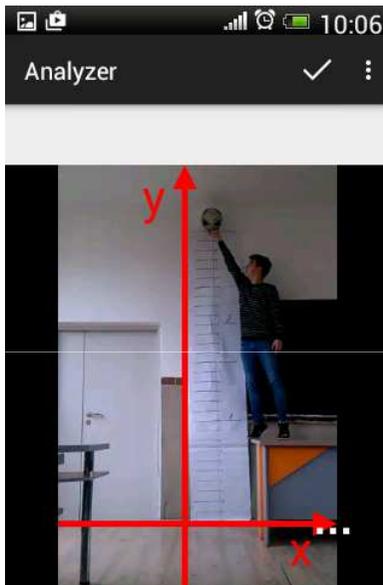
<https://play.google.com/store/apps/details?id=com.vidanalysis.free>



Record a video and import into the app.

Calibrate the video: mark the length of the known distance in the frame and insert the real length

# VidAnalysis



Pick the origin of the coordinate system.

Mark the ball by tapping on it in every frame.

Diagrams are generated automatically:  
 $x = f(t)$ ,  $y = f(t)$  and  $y = f(x)$   
 $v_x = f(t)$  and  $v_y = f(t)$

Data table

